

Total No. of Questions : 9]

SEAT No. :

P-9074

[Total No. of Pages : 4

[6178]-9

B.E.

ENGINEERING MATHEMATICS - II
(2019 Pattern) (Semester - II) (107008)

Time : 2½ Hours]

[Max. Marks : 70

Instructions to the candidates:

- 1) Question No. 1 is compulsory.
- 2) Solve Q. No. 2 or Q. No. 3, Q. No. 4 or Q. No. 5, Q. No. 6 or Q. No. 7, Q. No. 8 or Q. No. 9.
- 3) Neat diagrams must be drawn wherever necessary.
- 4) Figures to the right indicate full marks.
- 5) Use of electronic pocket calculator is allowed.
- 6) Assume suitable data, if necessary.

Q1) Write the correct option for the following multiple choice questions.

a) $\int_0^{2\pi} \sin^3 \theta \cos^4 \theta d\theta$ [2]

i) $\frac{2}{35}$

ii) $\frac{1}{15}$

iii) 0

iv) $\frac{2\pi}{35}$

b) The equation of tangents to the curve $3ay^2 = x(x - a)^2$, at the origin, if exist is [2]

i) $x = a$

ii) $x = 0, y = 0$

iii) $x = 0$

iv) $y = 0$

c) $\int_{\theta=0}^{\pi/2} \int_{r=0}^2 r dr d\theta =$ [2]

i) π

ii) 1

iii) 2

iv) $\frac{\pi}{2}$

P.T.O.

- Q4)** a) Trace the curve $y^2(2a - x) = x^3$, $a > 0$. [5]
 b) Trace the curve $r = a(1 - \cos\theta)$ [5]
 c) Find the arc length of cycloid $x = a(t + \sin t)$, $y = a(1 - \cos t)$ from one cusp to another cusp. [5]

OR

- Q5)** a) Trace the curve $xy^2 = a^2(a - x)$, $a > 0$ [5]
 b) Trace the curve $r = a\cos 3\theta$. [5]
 c) Trace the curve [5]

$$x^{2/3} + y^{2/3} = a^{2/3}$$

- Q6)** a) Show that the plane $2x + y + 2z = 6$ touches the sphere $x^2 + y^2 + z^2 - 6x - 6y - 6z + 18 = 0$. Also find the point of contact. [5]
 b) Find the equation of right circular cone whose vertex is at origin, axis is the line $\frac{x}{1} = \frac{y}{1} = \frac{z}{1}$ and has a semi-vertical angle of 30° . [5]

- c) Find the equation of right circular cylinder of radius 4 and axis is the line $\frac{x}{1} = \frac{y}{-1} = \frac{z}{1}$ [5]

OR

- Q7)** a) If the sphere $x^2 + y^2 + z^2 + 2\lambda x + 3\lambda y + 4\lambda z - 1 - 5\lambda = 0$ cuts the sphere $x^2 + y^2 + z^2 + 3x - 3y + 3z - 56 = 0$, orthogonally, then find the value of λ . [5]

- b) Find the equation of right circular cone whose vertex is at origin, generator is the line $\frac{x}{1} = \frac{y}{2} = \frac{z}{3}$ and axis is the line $\frac{x}{-1} = \frac{y}{1} = \frac{z}{2}$. [5]

- c) Find the equation of right circular cylinder of radius 2, whose axis passes through the origin and has direction ratios 1, -1, 1. [5]

- Q8)** a) Change order of integration and evaluate $\int_0^\infty \int_x^\infty \frac{e^{-y}}{y} dx dy$ [5]

- b) Find the area of cardioid $r = a(1 + \cos\theta)$ using double integration. [5]

- c) Prove that moment of inertia of the area included between curves $y^2 = 4ax$ and $x^2 = 4ay$ about x -axis is $\frac{144}{35}Ma^2$, given that density $\rho = \frac{3M}{16a^2}$ and M is the mass. [5]

OR

- Q9) a) Change following double integration to its polar form and evaluate

$$\iint_R \frac{x^2 y^2}{x^2 + y^2} dx dy, \text{ where } R \text{ is annulus between } x^2 + y^2 = 4 \text{ and } x^2 + y^2 = 9. \quad [5]$$

- b) Prove that the volume bounded by cylinders $y^2 = x$ and $x^2 = y$ and planes $z = 0$, $x + y + z = 2$ is $\frac{11}{30}$. [5]

- c) Find the x - co-ordinate of centre of gravity of a loop of $r = a \sin 2\theta$ in first quadrant, given that area of loop is $A = \frac{\pi a^2}{8}$. [5]

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